

**DIPLOMA EXAMINATION IN ENGINEERING/TECHNOLOGY/
MANAGEMENT/COMMERCIAL PRACTICE - NOVEMBER 2023**

ENGINEERING MATHEMATICS I

(Maximum Marks:100)

(Time: 3 hours)

PART - A

(Maximum Mark : 10)

Marks

I. Answer **all** the questions in one or two sentences. Each question carries 2 marks.

1. Evaluate $\lim_{x \rightarrow 0} \frac{2x-3}{3x+4}$

2. Find $\sin 60^\circ \cos 30^\circ + \cos 60^\circ \sin 30^\circ$

3. Find the area of a triangle given $b = 3\text{cm}$, $c = 2\text{cm}$ and $A = 30^\circ$

4. Find $\frac{dy}{dx}$ if $y = e^x \log x$

5. Find the range of values of x for which $y = 2x^2 - 8x + 1$ increasing (5 x 2 = 10)

PART - B

(Maximum Mark: 30)

II Answer **any five** questions from the following. Each question carries 6 marks.

1. Express $\sqrt{3} \cos x + \sin x$ in the form $R \sin (x + \alpha)$ where α is acute.

2. Find the value of $\tan 75^\circ$ without using tables and hence show that
 $\tan 75^\circ + \cot 75^\circ = 4$

3. Prove that $R (a^2 + b^2 + c^2) = abc (\cot A + \cot B + \cot C)$.

4. Differentiate $\cos x$ by the method of first principle.

5. If $x = \frac{1-t^2}{1+t^2}$ $y = \frac{2t}{1+t^2}$ Find $\frac{dy}{dx}$?

6. Find the equation of the tangent and normal to the curve $y = x^2 + x - 1$ at (2,5)

7. A cylindrical can open at one end is to have a volume of $64\pi \text{ cm}^3$. Find the radius and height of the cylinder such that the metal used its minimum?

(5 x 6 = 30)

PART – C

(Maximum Mark: 60)

(Answer **one full** question from each unit. Each full question carries 15 marks.)

UNIT – 1

III. a) If $\cos A = \frac{3}{5}$ $\tan B = \frac{5}{12}$ A & B are acute angles.

Find $\sin(A+B)$ & $\cos(A+B)$. (5)

b) prove that $\frac{\sec \theta}{\sec \theta - 1} + \frac{\sec \theta}{\sec \theta + 1} = 2 \operatorname{Cosec}^2 \theta$ (5)

c) Prove that $\frac{\cos(90+A) \sec(360+A) \tan(180-A)}{\sec(A-720) \sin(540+A) \cot(A-90)} = 1$ (5)

OR

IV. a) Prove that $\sin(A+B) \sin(A-B) = \sin^2 A - \sin^2 B$ (5)

b) If $\theta = 30^\circ$, Verify that $\tan 2\theta = \frac{2 \tan \theta}{1 - \tan^2 \theta}$ (5)

c) The horizontal distance between two towers is 50m and the angle of depression of the first tower as seen from the second which is in 150m height is 60° . Find the height of the first tower? (5)

UNIT – II

V. a) Prove that $\frac{1 + \cos 2A}{\sin 2A} = \cot A$ and deduce the value of $\cot 15^\circ$. (5)

b) Show that $\cos 55^\circ + \cos 65^\circ + \cos 175^\circ = 0$ (5)

c) Solve $\triangle ABC$ given $a = 5\text{cm}$, $b = 8\text{cm}$ $c = 30^\circ$ (5)

OR

VI. a) Prove that $\sin 10^\circ \sin 30^\circ \sin 50^\circ \sin 70^\circ = \frac{1}{16}$ (5)

b) Prove that $2(bc \cos A + ca \cos B + ab \cos c) = a^2 + b^2 + c^2$ (5)

c) Two angles of a triangular plot of land are $53^\circ 17'$ and $67^\circ 9'$ the side between them is measured to be 100m. How many meters of fencing is required to fence the plot? (5)

UNIT – III

VII. a) Evaluate $\lim_{x \rightarrow a} \frac{x^{1/2} - a^{1/2}}{x^{1/3} - a^{1/3}}$ (5)

b) If $y = a \sin mx$ prove that $y'' + m^2 y = 0$ (5)

c) If $y = a \cos(\log x) + b \sin(\log x)$ show that $\frac{x^2 d^2 y}{dx^2} + \frac{x dy}{dx} + y = 0$ (5)

OR

VIII. a) Evaluate $\lim_{x \rightarrow 5} \frac{x^3 - 125}{x^2 - 25}$ (5)

b) Find $\frac{dy}{dx}$ if (i) $x = at^2$ $y = 2at$

(ii) $y = \frac{\sin 2x}{1 + \cos 2x}$ (5)

c) If $y = \sin^{-1} x$ P.T. $(1-x^2) \frac{d^2y}{dx^2} - x \frac{dy}{dx} = 0$ (5)

UNIT - IV

IX. a) The displacement of a body is given by $x = 3 \cos 4t + 5 \sin 4t$. Show that the acceleration varies as the distance. (5)

b) Find the maximum and minimum value of $4x^3 + 9x^2 - 12x + 2$ (5)

c) A Circular plate of radius 3 inches expands when heated at the rate of 2 inch/sec. Find the rate at which the area of the plate is increasing at the end of 3 sec? (5)

OR

X. a) For what values of x is the tangent to the curve $\frac{x}{x^2+1}$ is parallel to the x – axis. (5)

b) The perimeter of a rectangle is 100m. Find the sides when the area is maximum? (5)

c) A balloon is spherical in shape. Gas is escaping from it at the rate of 10cc/Sec. How fast is the surface area shrinking when the radius is 15cm? (5)

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